

Varianta 28

III.

13. a) Fie x numărul copiilor. Obiectul costă $20x + 5$ lei, respectiv $30x - 25$ lei, deci

$$20x + 5 = 30x - 25 \Rightarrow 10x = 30 \Rightarrow x = 3.$$

b) Obiectul costă $20 \cdot 3 + 5 = 65$ lei.

14. a) $2 + a = \frac{5}{2} \Rightarrow a = \frac{1}{2}; \frac{3}{2} - b = \frac{5}{2} \Rightarrow b = -1.$

b) $f(x) = 2x + \frac{1}{2}$ și $S = \left(2 \cdot 1 + \frac{1}{2}\right) + \left(2 \cdot 2 + \frac{1}{2}\right) + \left(2 \cdot 3 + \frac{1}{2}\right) + \dots + \left(2 \cdot 20 + \frac{1}{2}\right) = 430.$

c) $2x + \frac{1}{2} \leq 2 \cdot \left(\frac{3}{2}x + 1\right) + 1 \Rightarrow x \in \left[-\frac{5}{2}; +\infty\right).$

15. b) $\frac{l^3 \sqrt{3}}{4} = 54\sqrt{3} \Rightarrow l^3 = 6^3 \Rightarrow l = 6 \Rightarrow AB = 6 \text{ cm}.$

c) Fie M mijlocul laturii $AB \Rightarrow MC \perp AB; MC \perp BB' \Rightarrow MC \perp (ABB')$

$MC \subset (MCB') \Rightarrow (MCB') \perp (ABB').$

d) $V_{MBCB'} = 9\sqrt{3} \text{ cm}^3. V_{MBCB'} = A_{MCB'} \cdot d(B; (MCB')) \cdot \frac{1}{3} \Rightarrow d(B; (MCB')) = \frac{6\sqrt{5}}{5} \text{ cm}.$